

# Analysis of the Reactivity Loss of the Phenix Core Cycles for the Experimental Validation of the DARWIN-FR Code Package

**Mr. Victor Viallon**  
CEA/IRESNE, France  
28 February 2024

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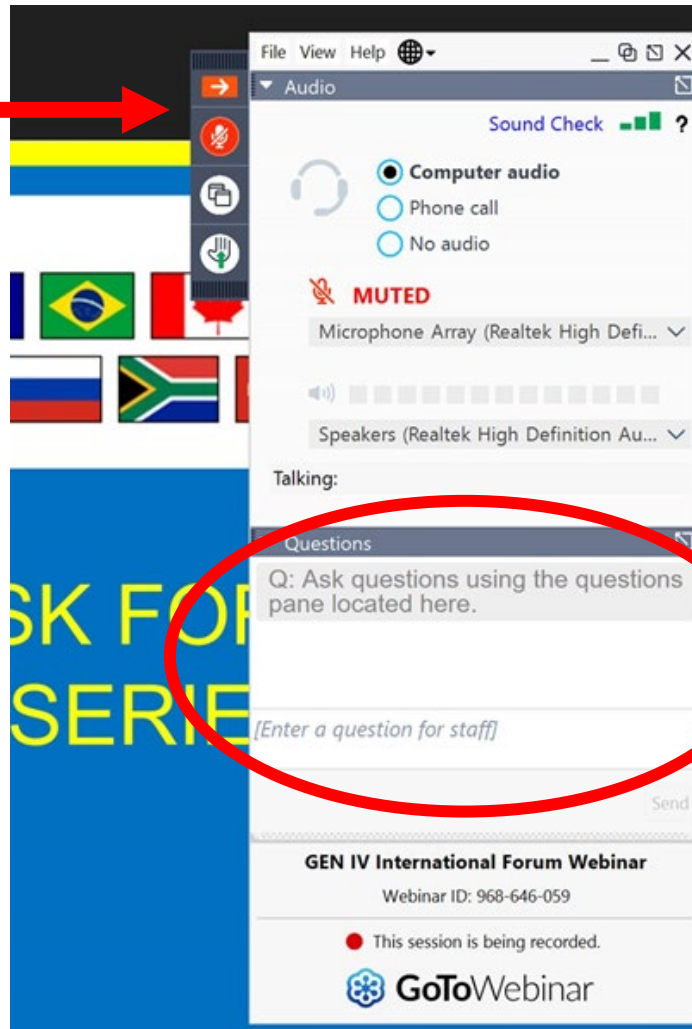
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# Analysis of the Reactivity Loss of the Phenix Core Cycles for the Experimental Validation of the DARWIN-FR Code Package

**Mr. Victor Viallon**

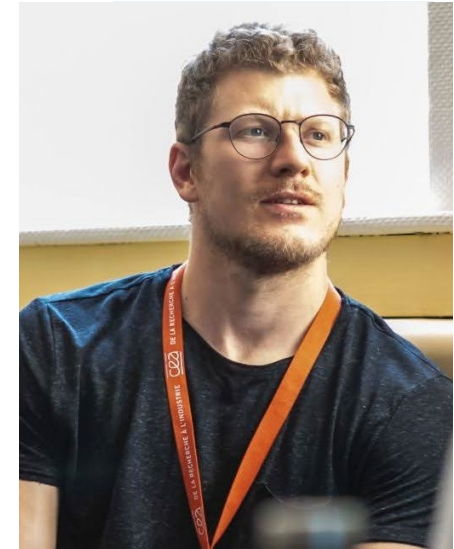
PhD work supervised and directed by **Elias-Yammir Garcia-Cervantes** and **Laurent Buiron**

**CEA/IRESNE, France**  
**28 February 2024**

# Meet the Presenter

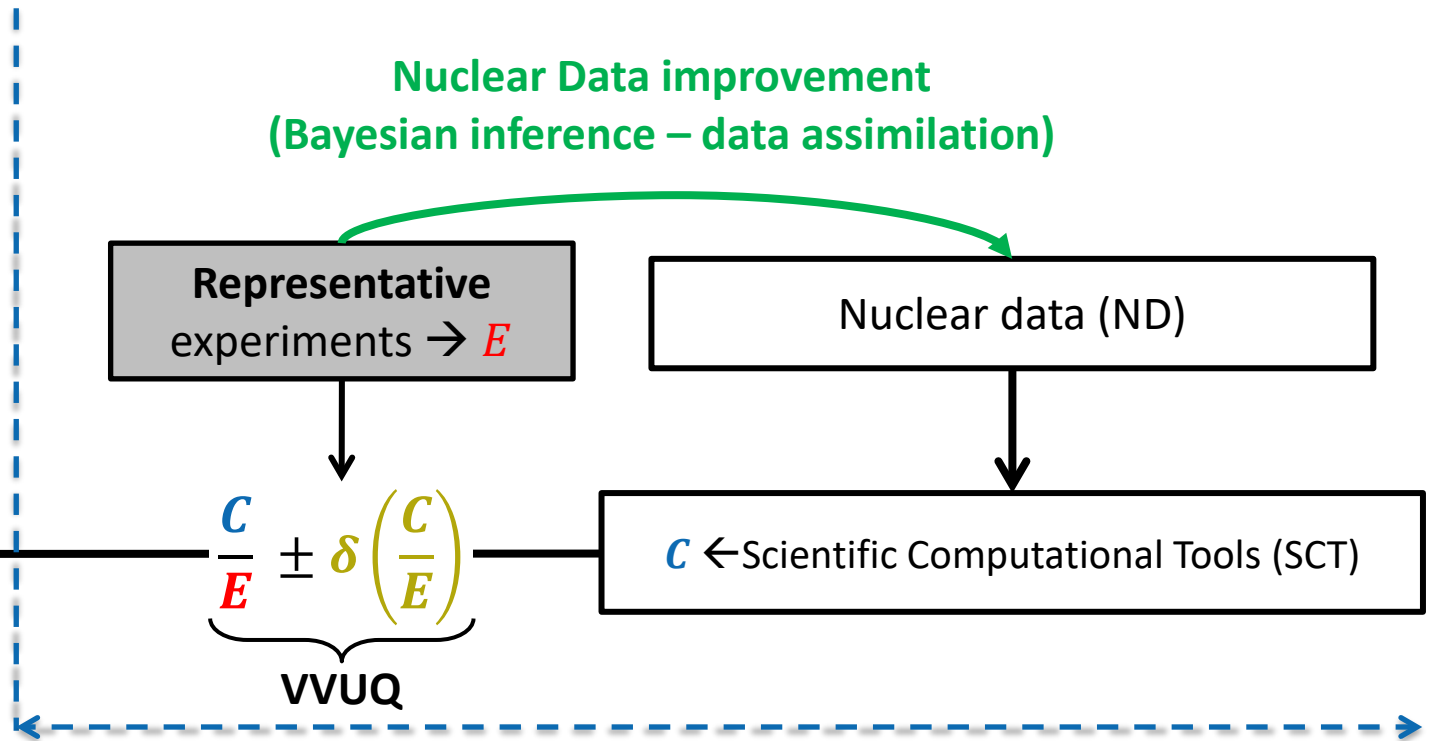
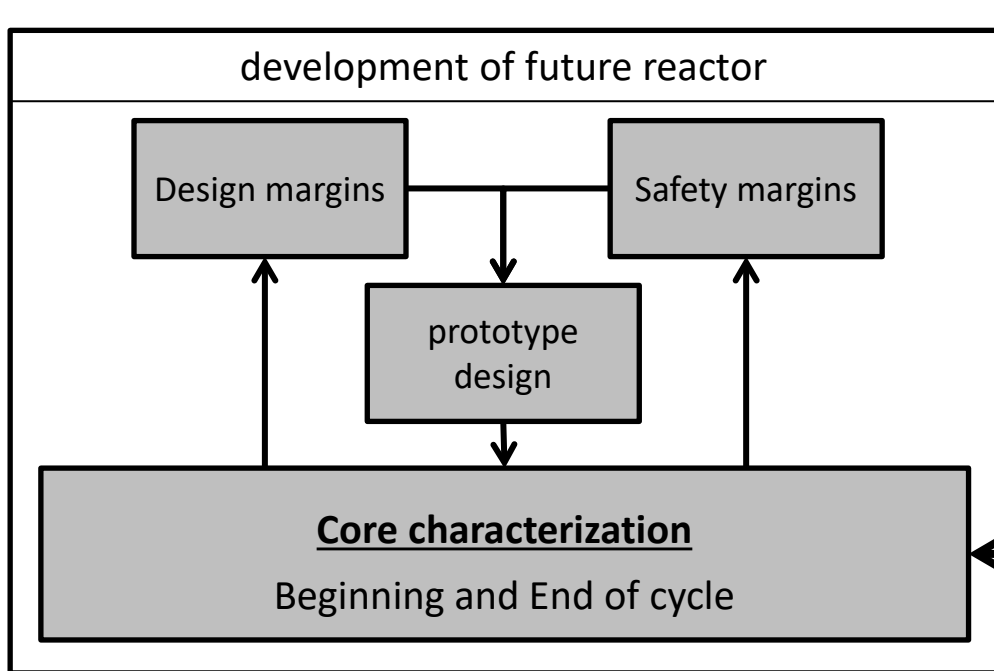
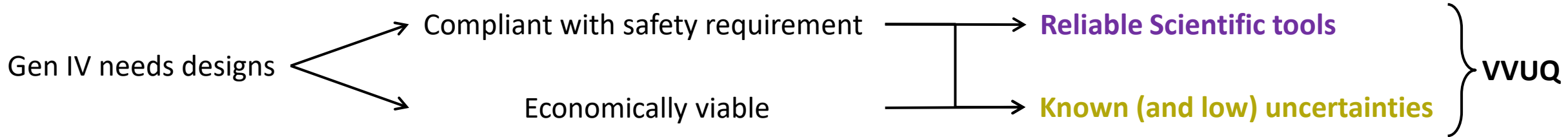
## Mr. Victor Viallon

- 3<sup>rd</sup> year PhD Student in the Research Institute for Nuclear Systems for low-carbon Energy Production (IRESNE) at CEA Cadarache, France
- Master degree in mechanics and industrial risk control engineering degree from the Centre-Val de Loire National Institute of Applied Sciences (INSA CVL)
- Advanced graduate degree in nuclear Engineering from the French Institute for Energy and Health Technologies (INSTN)



# Context

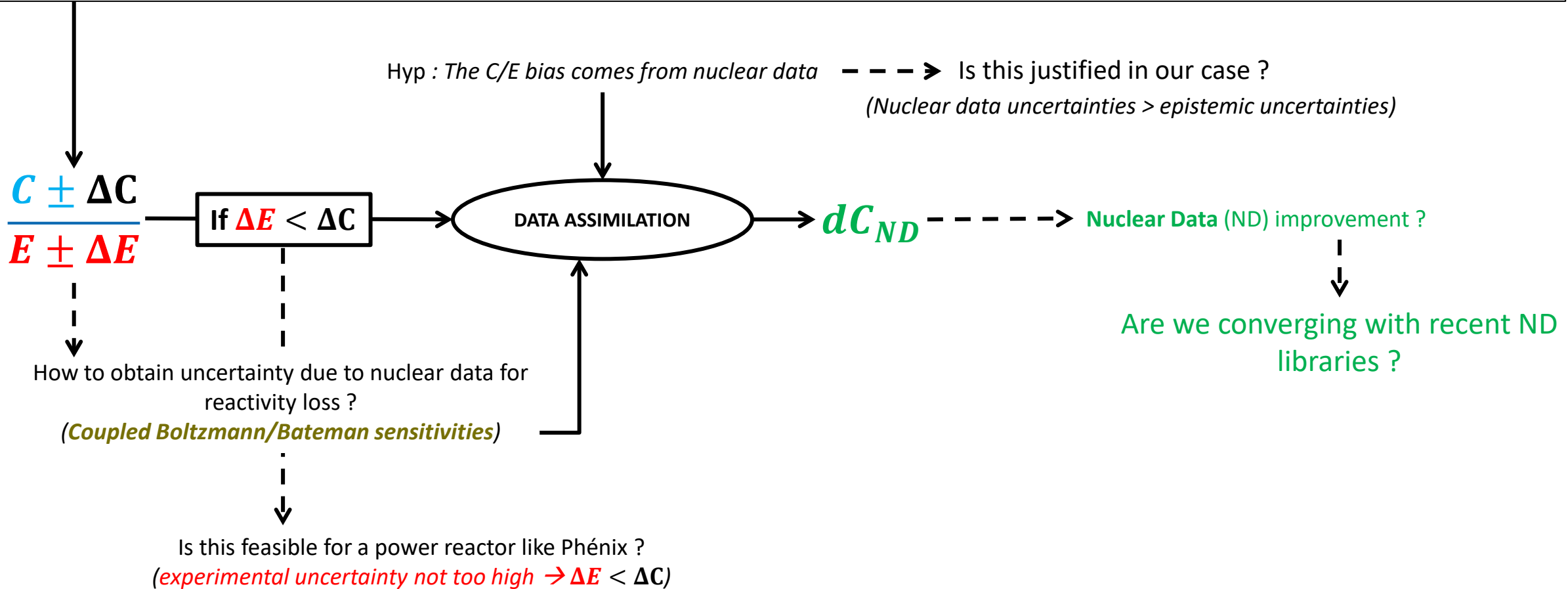
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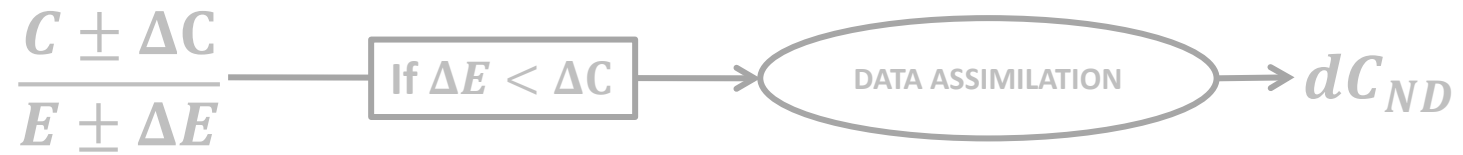
# Context

**Reactivity loss** : Fuel wear speed / Time cycle → Core economics  
 Related to End of cycle core characterization → Safety  
 Can provide information for fast Fission Yield → Science

Analysis of the **Reactivity Loss** of the **Phenix** Core Cycles for the **Experimental Validation** of the **DARWIN-FR Code Package**



# Context





**1** ■

# Phenix cycle simulation with DARWIN-FR package

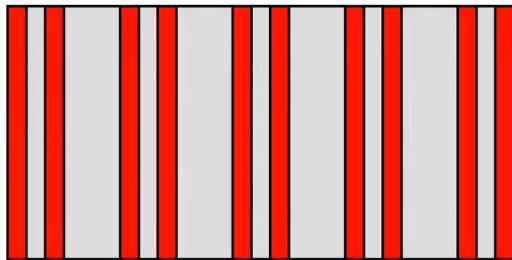
# Simulation of Phenix cycles with the DARWIN-FR code package

## What is reactivity loss ?

Multiplication factor :  $k_{eff} = \frac{\text{Number of neutron produced by fission}}{\text{Number of neutron absorbed and leaked}}$

Reactivity :  $\rho = \frac{k_{eff} - 1}{k_{eff} \cdot \beta_{eff}}$  [\$] Criticality :  $k_{eff} = 1 \mid \rho = 0$

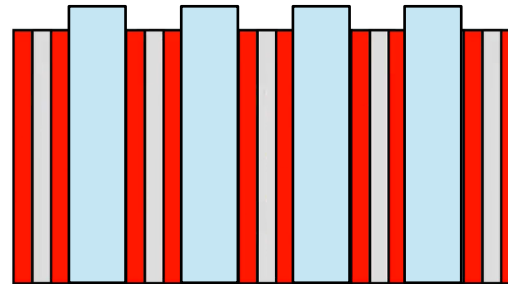
hypothetical **Supercritical**  
(forbidden to have  $\rho > 50\phi$ )



**Reactivity excess**

$$\rho = 10 \$$$

**Subcritical**

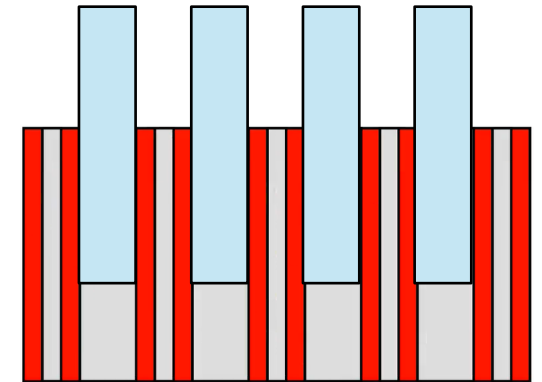


**Control rods to temper the reactivity excess and pilot the reactor reactivity**

$$\rho = \text{Reactivity excess} - \text{Control rods worth}$$

$$\rho = 10\$ - 20\$ = -10\$$$

**Critical**



$$\rho = 10\$ - 10\$ = 0\$$$

Neutronics for reactor physics = How and how much is the **reactivity affected**

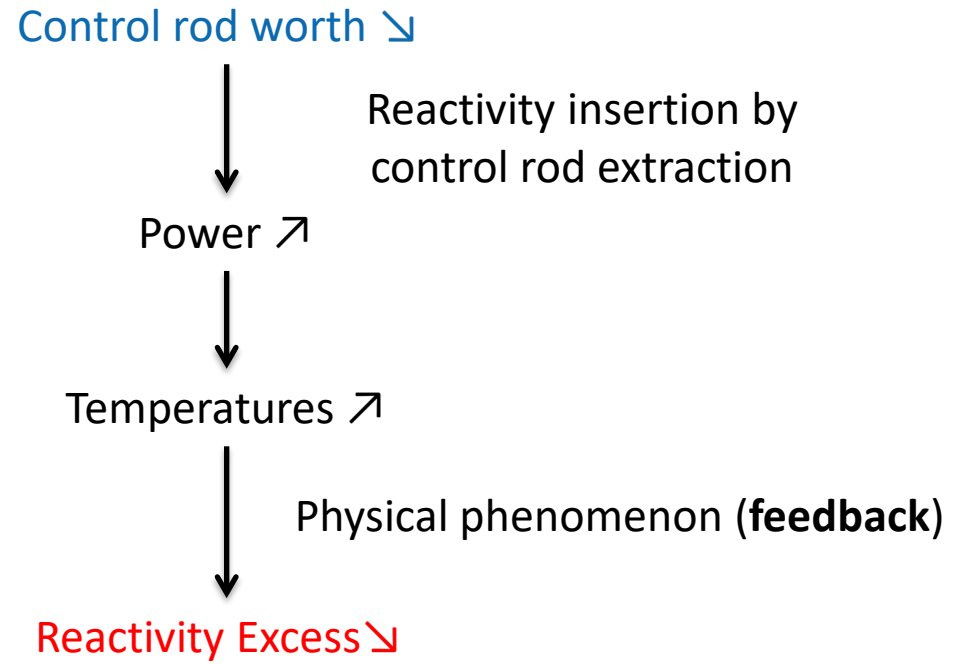
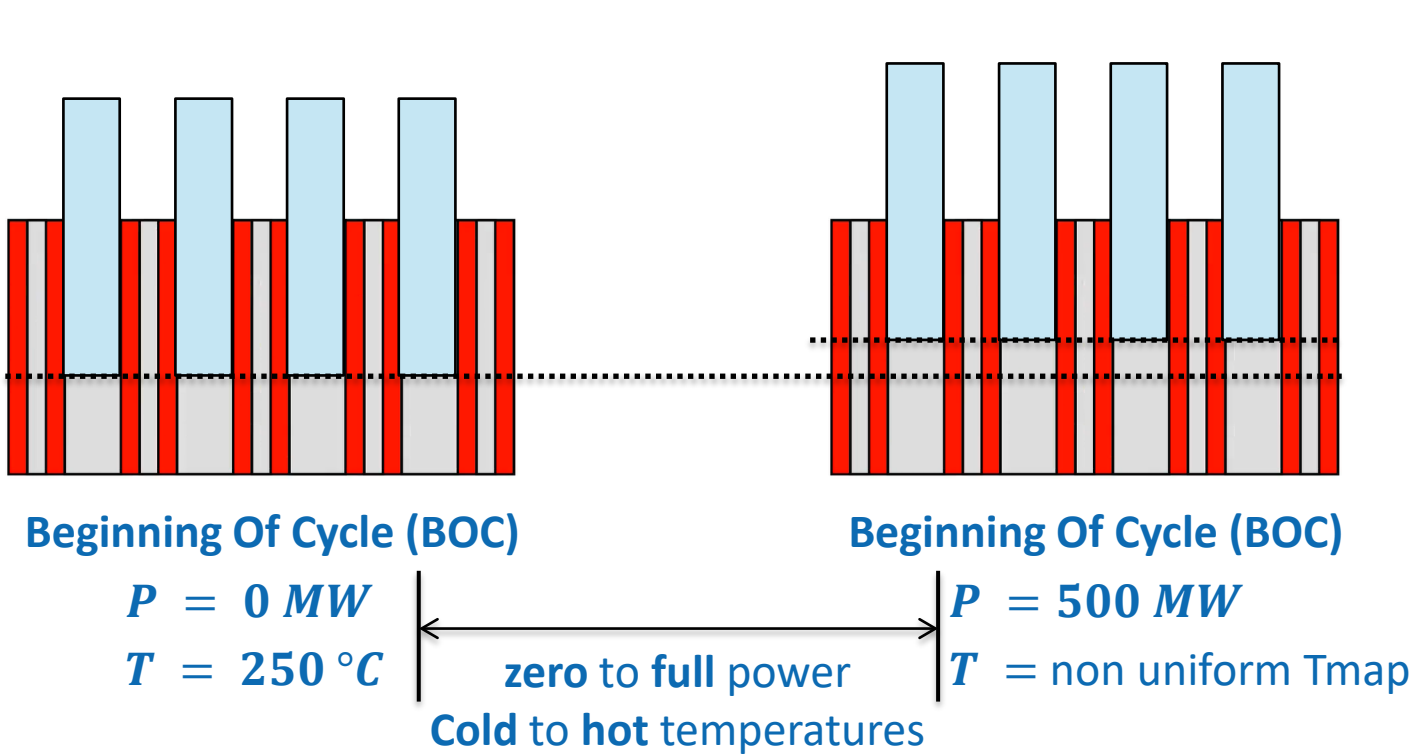
by self-induced physical phenomena on the reactivity excess (fuel depletion, sodium void, T, ...)

by operator induced phenomenon on the control rod worth

# Simulation of Phenix cycles with the DARWIN-FR code package

## What is reactivity loss ?

in normal operation  $\rightarrow \rho = \text{Reactivity excess} - \text{Control rods worth} = 0$

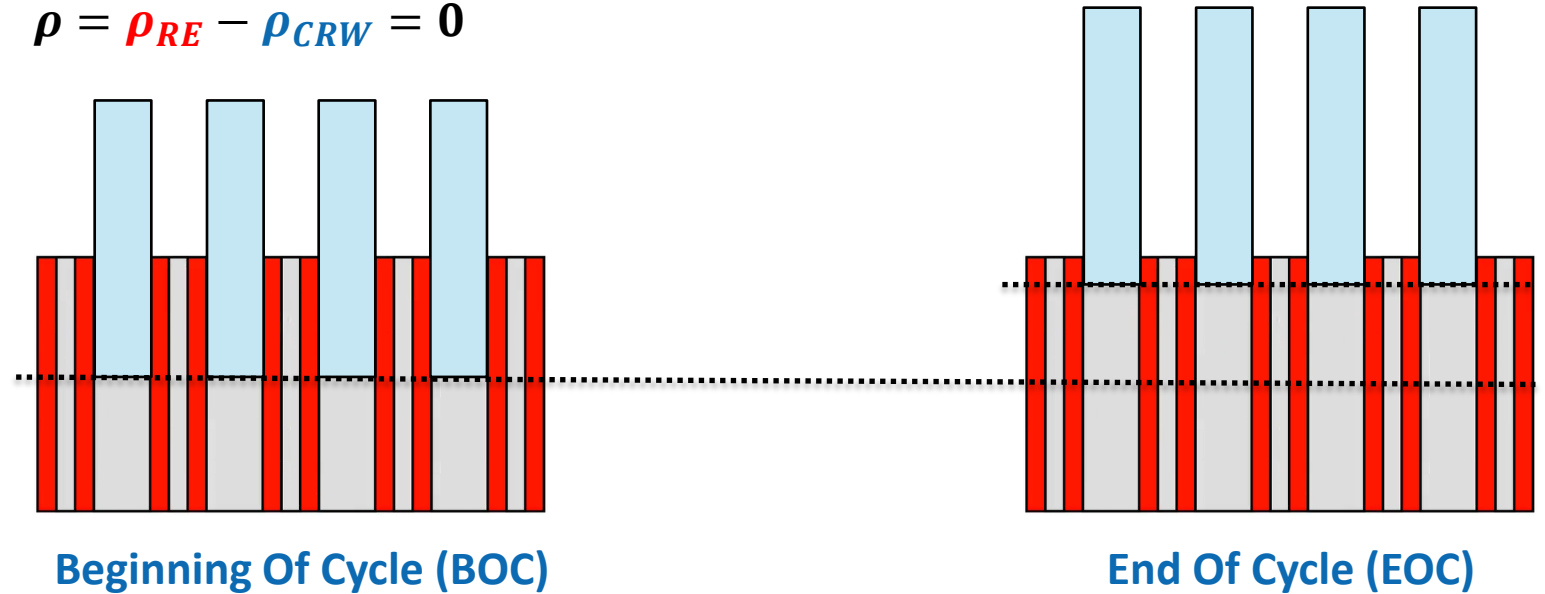
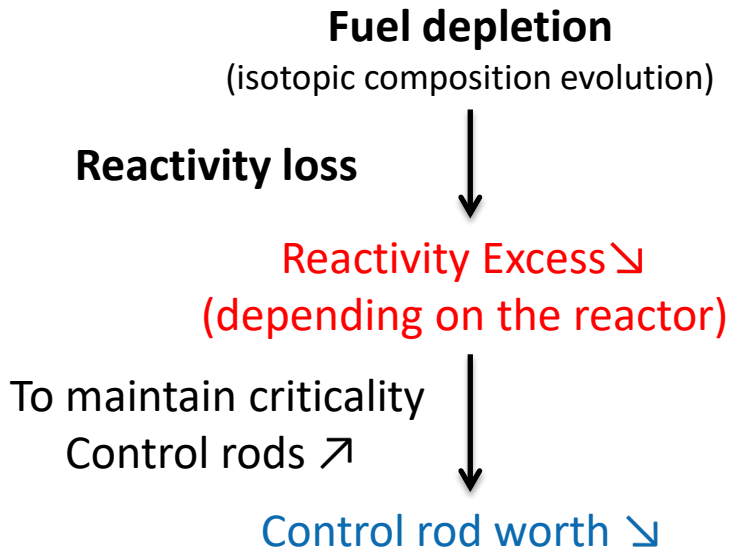


# Simulation of Phenix cycles with the DARWIN-FR code package

## What is reactivity loss ?

in normal operation  $\rightarrow \rho = \text{Reactivity excess} - \text{Control rods worth} = 0$

$$\rho = \rho_{RE} - \rho_{CRW} = 0$$



### Fuel depletion

what's the new isotopic composition ?  
Does the total feedback change ?



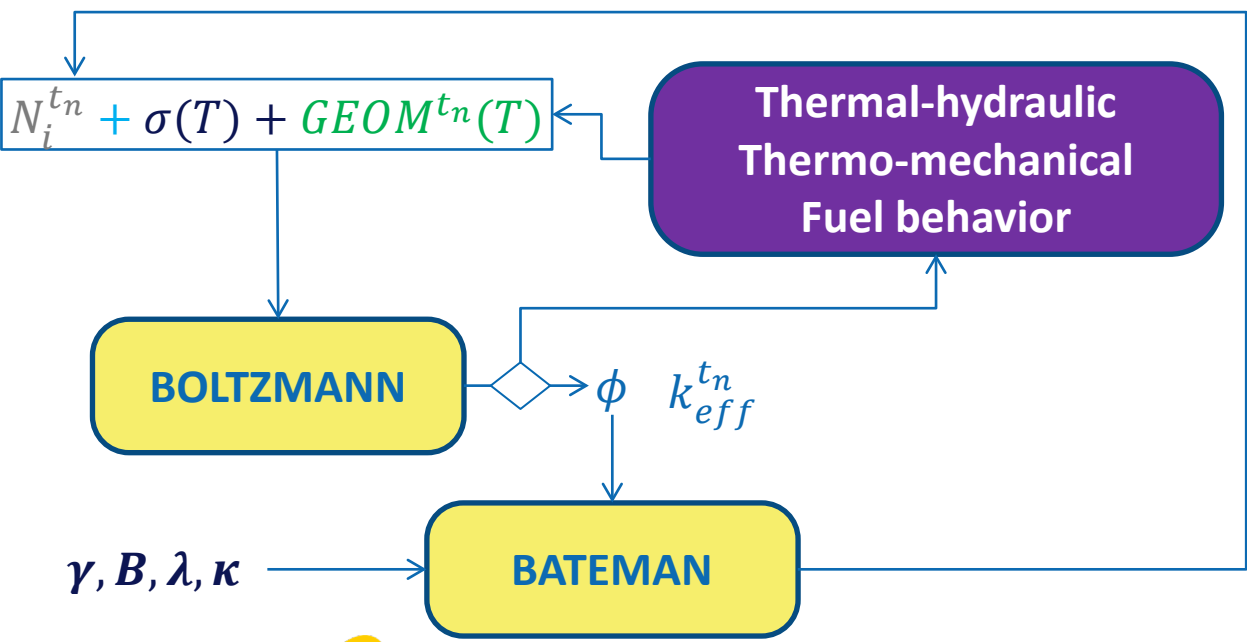
# Simulation of Phenix cycles with the DARWIN-FR code package

## How to compute reactivity loss ?

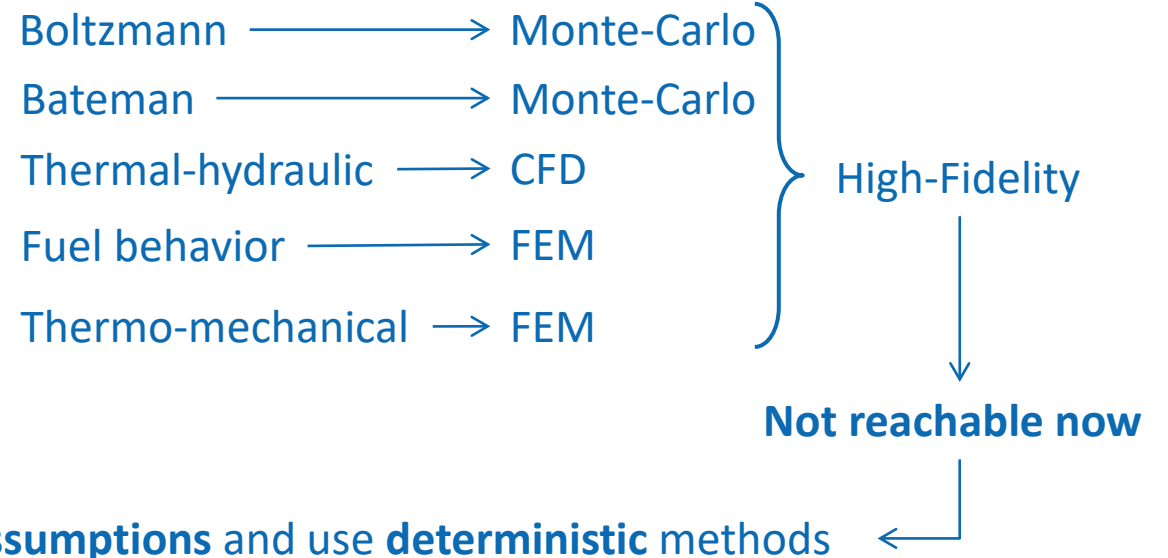
BATEMAN  $\rightarrow N_i(\vec{r}, t) = g(\tau(\vec{r}, \phi(\vec{r}, E, \Omega, t), \kappa, \sigma(E, T)), \gamma_I, B, \lambda)$

BOLTZMANN  $\rightarrow \phi(\vec{r}, E, \Omega, t) = f(N_i(\vec{r}, t, T), \sigma(E, T), \partial\omega(T))$

Coupled equations  $\dashrightarrow$  Quasi-static hypothesis  
 (Boltzmann stationary + Constant flux depletion)



Reactivity loss coefficient :  $\alpha_{BU} = \frac{d\rho_{RE}}{dt}$



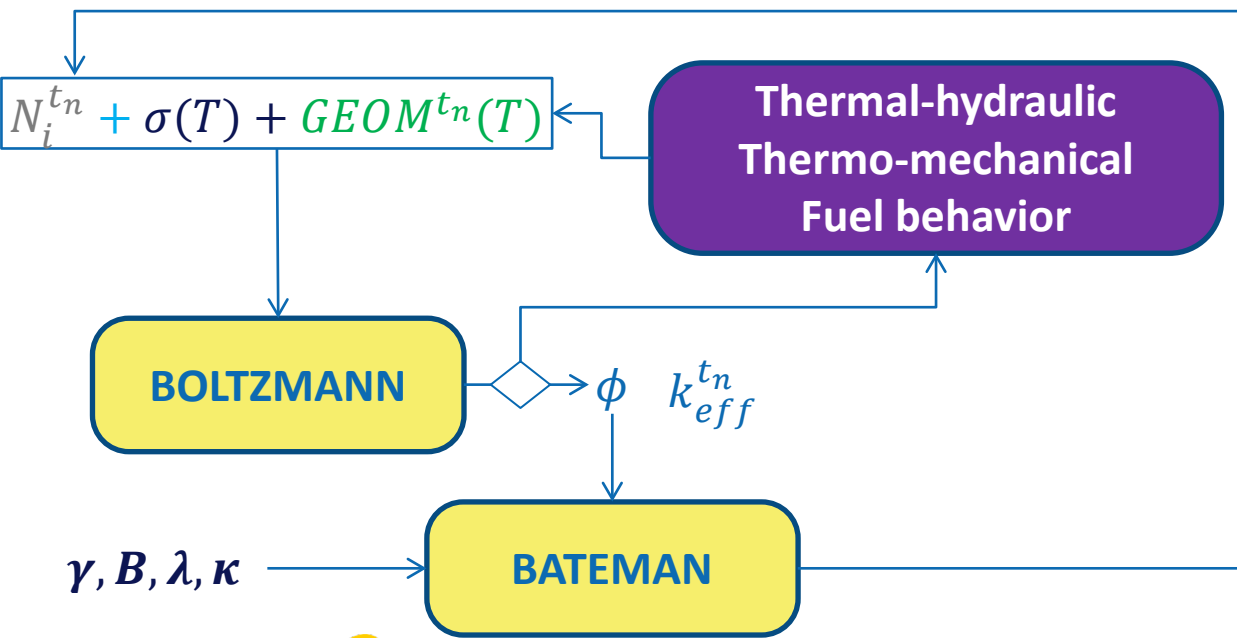
# Simulation of Phenix cycles with the DARWIN-FR code package

## How to compute reactivity loss ?

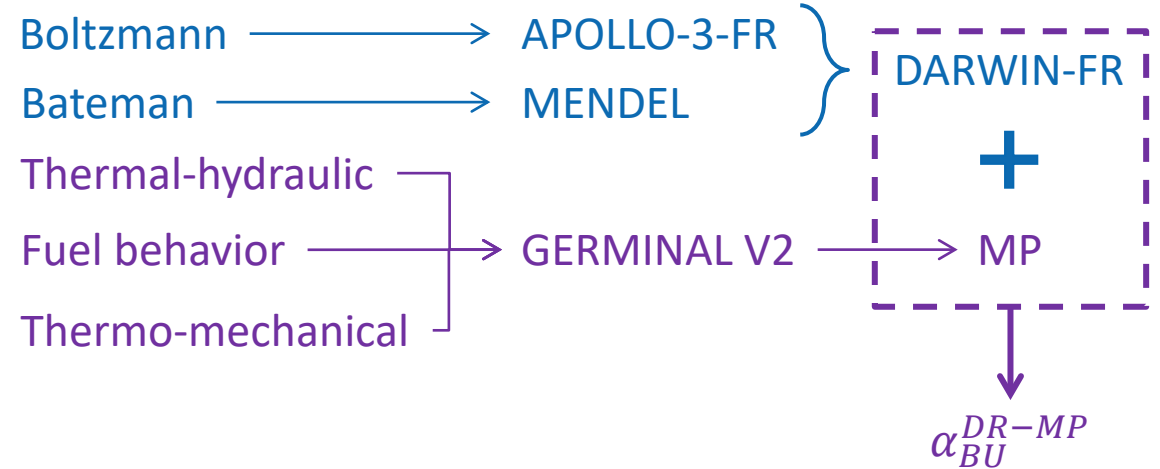
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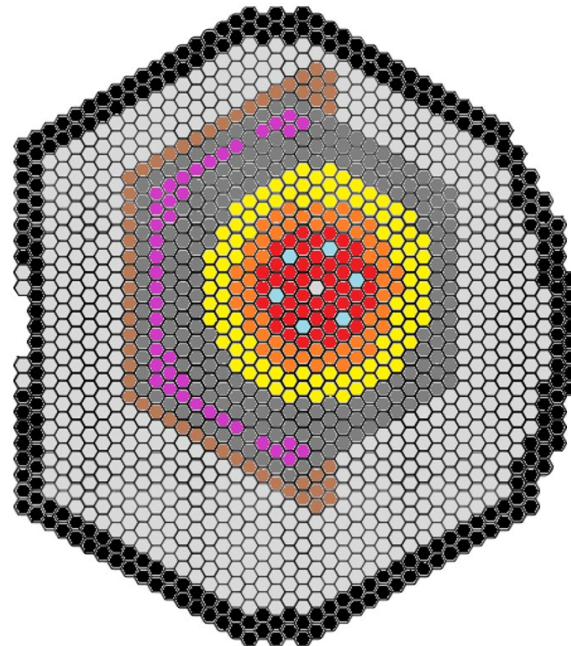
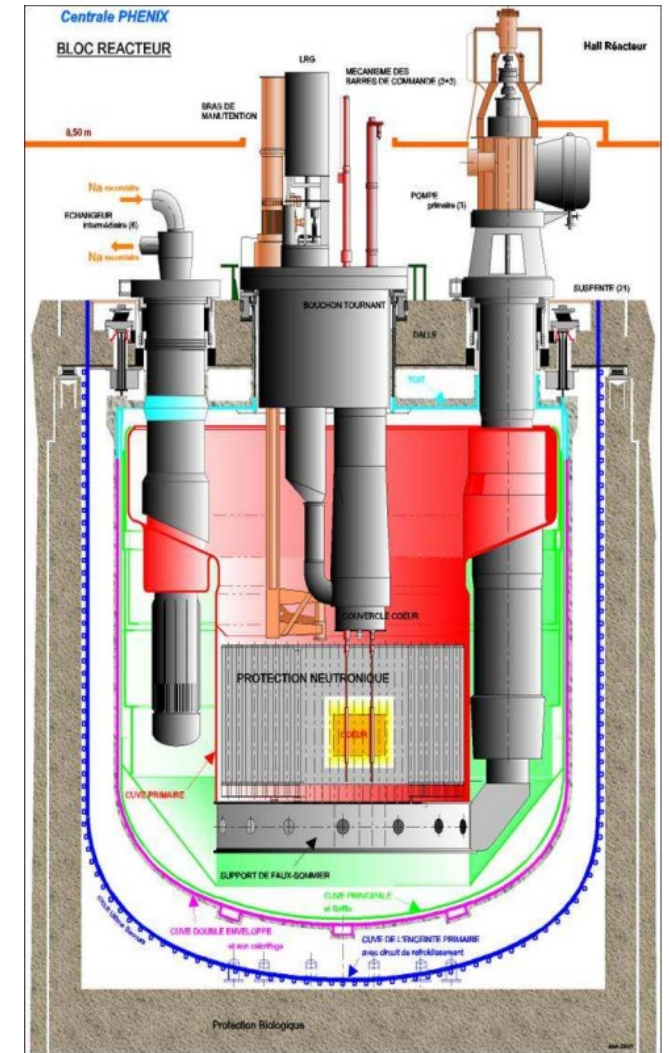


# Simulation of Phenix cycles with the DARWIN-FR code package

## Phenix reactor



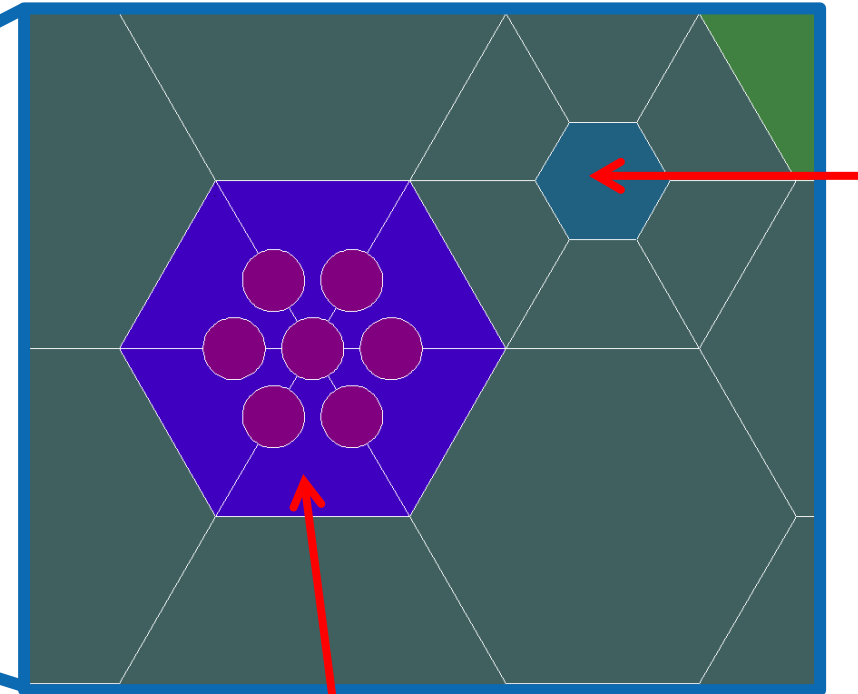
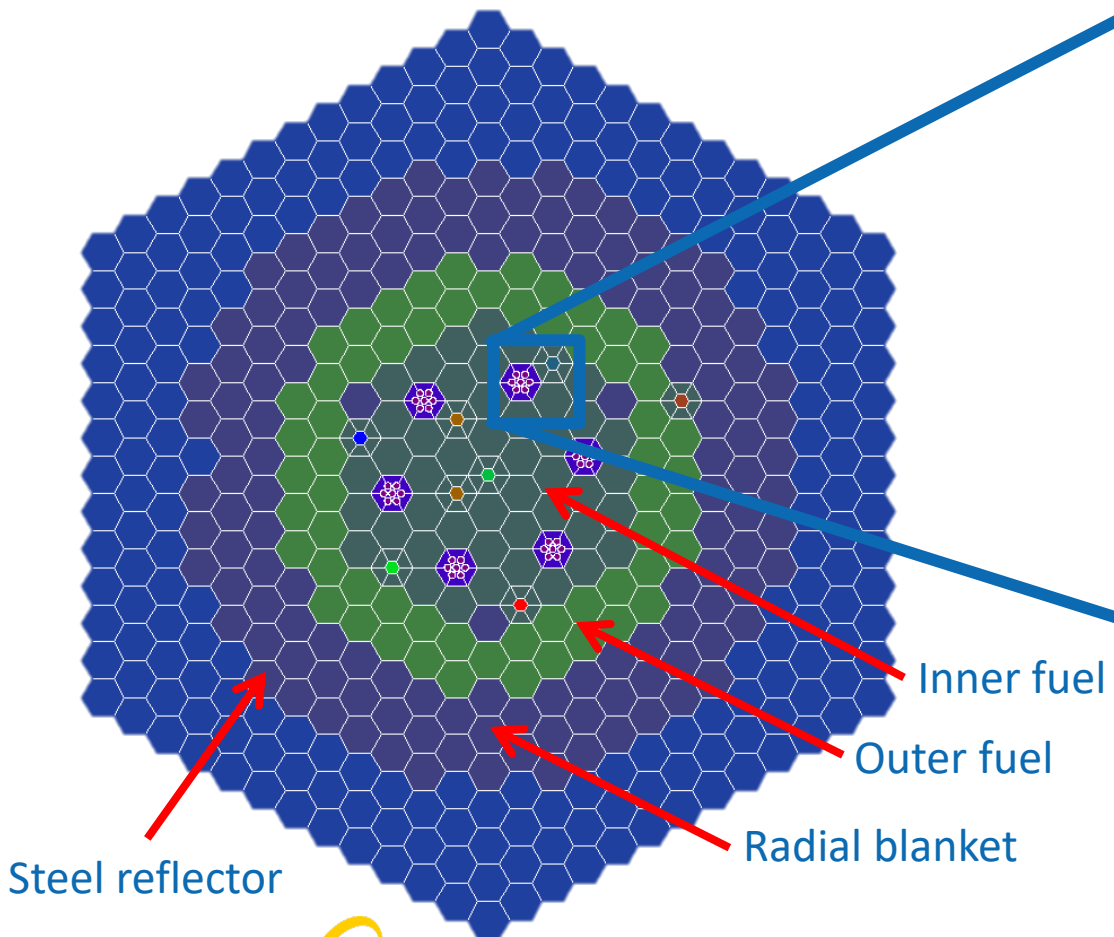
CEA Marcoule, France  
Pool-type Sodium cooled Fast Reactor – 563 MWth  
35 operational years – more than 50 cycles  
100 fissile subassemblies  
150 fertile blanket subassemblies  
6 control rods  
**In-core experiments** for irradiation purpose





# Simulation of Phenix cycles with the DARWIN-FR code package

## Study of the cycle 42 with DARWIN-FR



modeling of in-core experiments

Semi-heterogeneous control rod modeling

Complex object to represent

Best Estimate  $\longrightarrow \alpha_{BU}^{DR-MP} = -4.650 \text{ ¢/EFPD}$



# Simulation of Phenix cycles with the DARWIN-FR code package

## DARWIN-FR bias decomposition

“Real” value / experimental value

$$\widehat{E} = \underbrace{C_{HF}} + \underbrace{dC_{ND} + dC_{MPdata}}$$

Equations “perfectly” solved

Error made by using **assumed** rather than the “real” input data (**uncertainties**)

$$C_{HF} = \underbrace{C^{DR-MP}} + \underbrace{\Delta C_{AP3} + \Delta C_{MP} + \Delta C_{Ni^0} + \Delta C_{chain} + \Delta C_{tech} + \Delta^2(\dots) + \dots}_{\Delta C}$$

Equations solved with assumptions

**Epistemic uncertainties** (error made with assumptions) =  $\Delta C$

**Bias decomposition = Estimate epistemic uncertainties**

# Simulation of Phenix cycles with the DARWIN-FR code package

## DARWIN-FR bias decomposition

$$\alpha_{BU}^{DR-MP} = -4.650 \text{ ¢/EFPD}$$

$\Delta C_{MP} \approx 0 \%$  MP coupling contribution **0.9%** → Uncertainty over this (low) contribution → negligible

$\Delta C_{N_i^0} \approx 0 \%$  Database validated on BOC reactivity + Cycles done with D3R until cycle 48 and no difference between computed and initialized  $N_i^0$

$\Delta C_{tech} \approx 0 \%$  Cycle stable so the geometry doesn't change (significantly) during irradiation

$\Delta C_{chain} \approx 0 \%$  Chain depletion (29 HN – 150 FP / instead of several thousands) developed for reactivity loss and validated in [Foissy 2020]

$\Delta^{n \geq 2} \approx 0 \%$  Assumption

$\Delta C_{AP3} \approx 0 \%$  BOC reaction rate comparison between APOLLO-3-FR and the reference Monte-Carlo tool TRIPOLI-4®  
**To be investigated in depth**

# Simulation of Phenix cycles with the DARWIN-FR code package

## DARWIN-FR bias decomposition



# 2.

## Experimental reactivity loss

# Experimental reactivity loss

What is reactivity loss ?

$$\rho_{RE}^{EOC} - \rho_{RE}^{BOC} = \rho_{CRW}^{EOC} - \rho_{CRW}^{BOC}$$

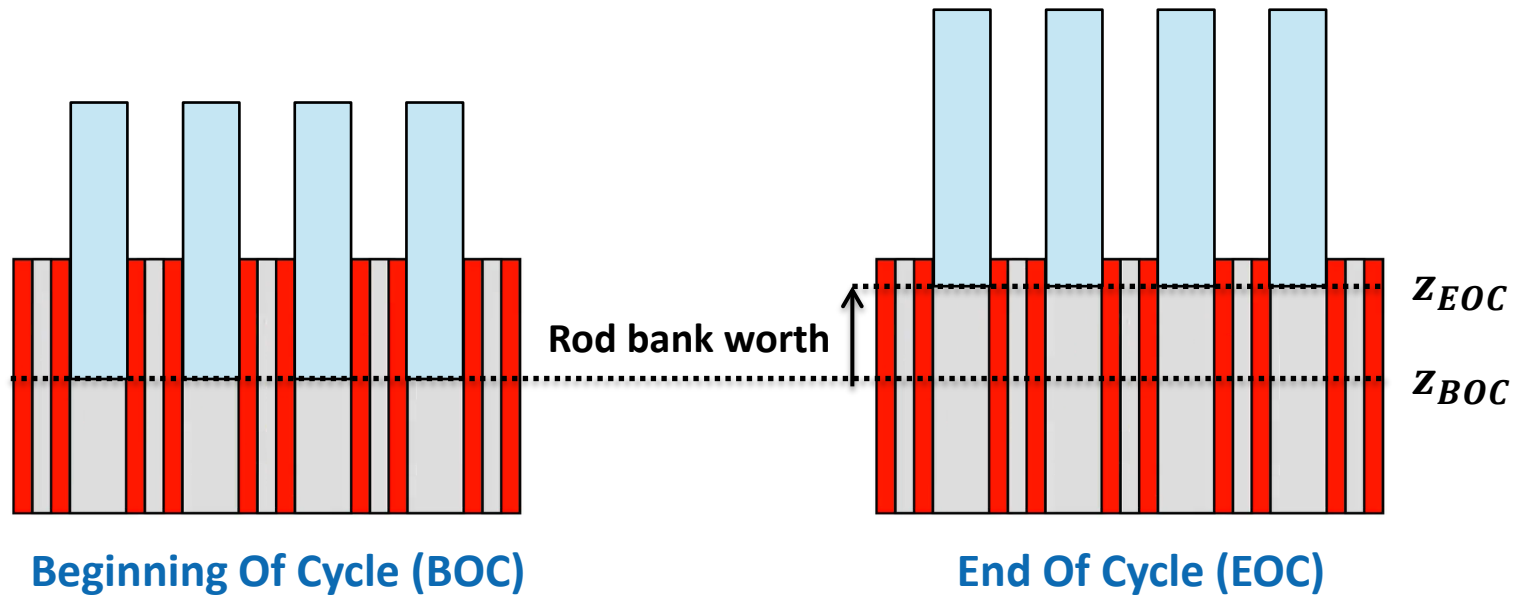
Reactivity loss = Rod Bank worth between  $z_{BOC}$  and  $z_{EOC}$



$z(t) ?$

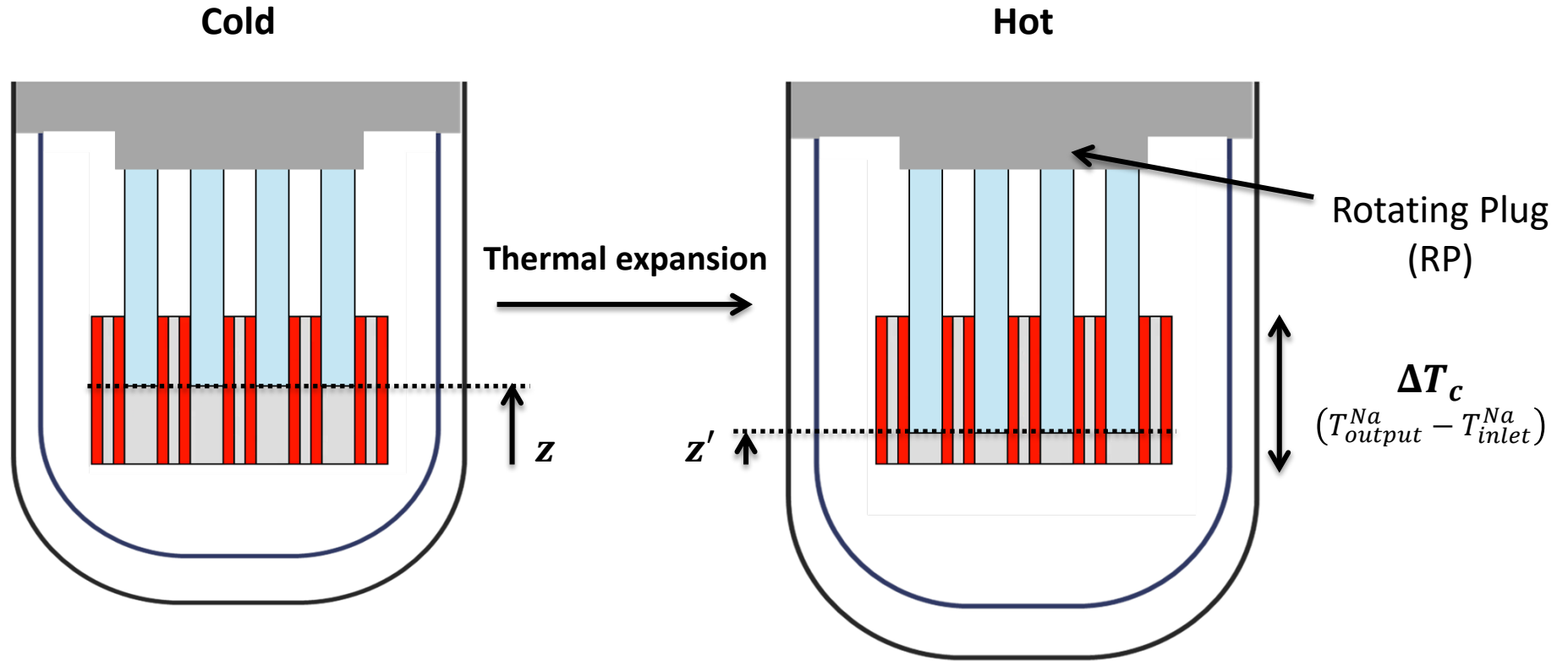
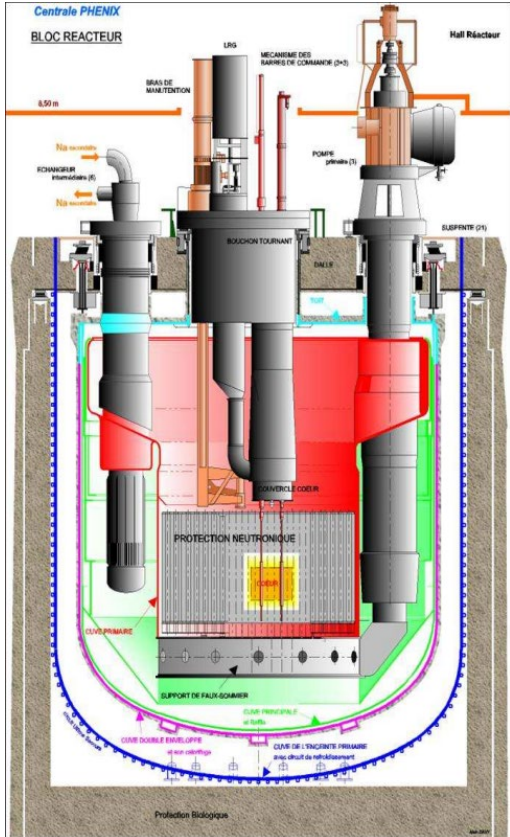
$\rho_{RB}(z) ?$

$$\rho = \rho_{RE} - \rho_{CRW} = 0$$



# Experimental reactivity loss

Axial position history of the Rod Bank through irradiation cycle → fundable inside cycle report, BUT...



$$z' = f_{expansion}(z, \Delta T_c, T_{RP}) = z + A \cdot \Delta T_c + B \cdot (T_{RP} - C) + D$$

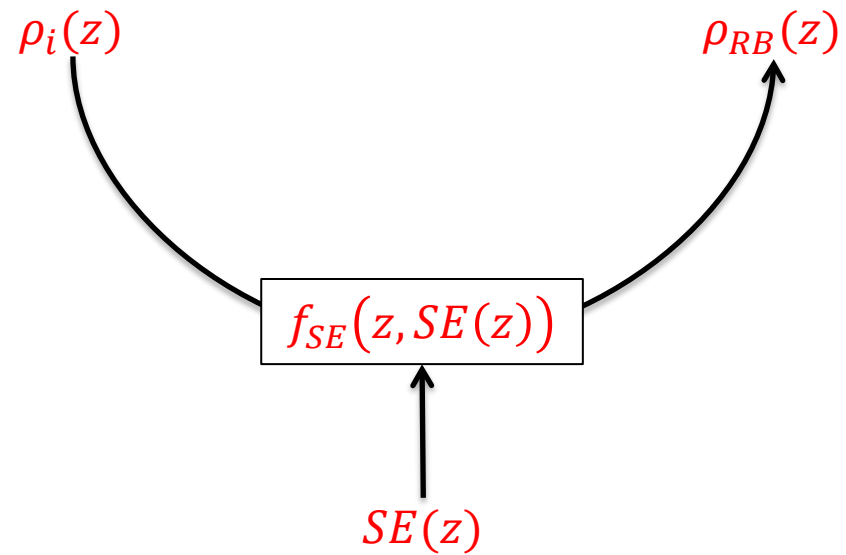
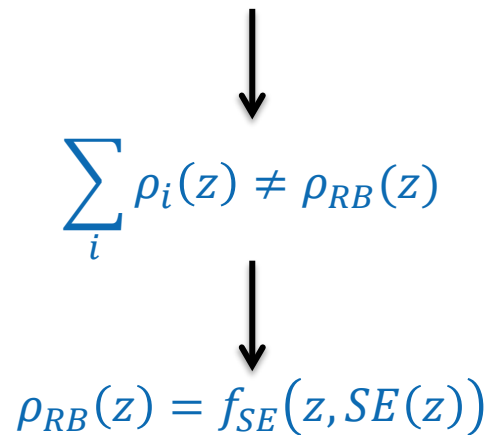
The axial position must be corrected to take into account thermal expansion

# Experimental reactivity loss

## How to obtain the rod bank worth through axial position ( $\rho_{RB}(z)$ )

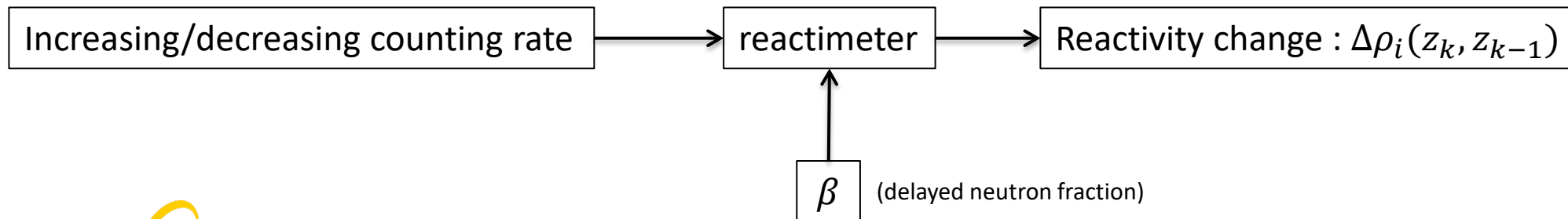
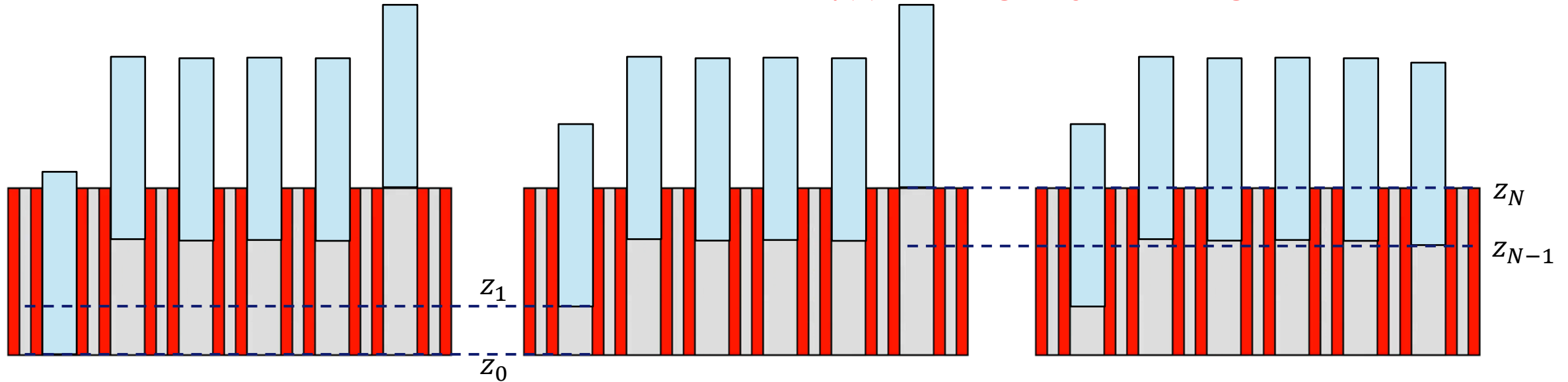
Not possible to measure directly the rod bank worth for the upper part of the core ☹️

Possible to only measure directly individual control rod worth  $\rho_i(z)$  and collapse them into the  $\rho_{RB}(z)$  by taking into account the **shadow effect**



# Experimental reactivity loss

How to obtain each individual control rod worth  $(\rho_i(z)) \rightarrow$  weight by balancing

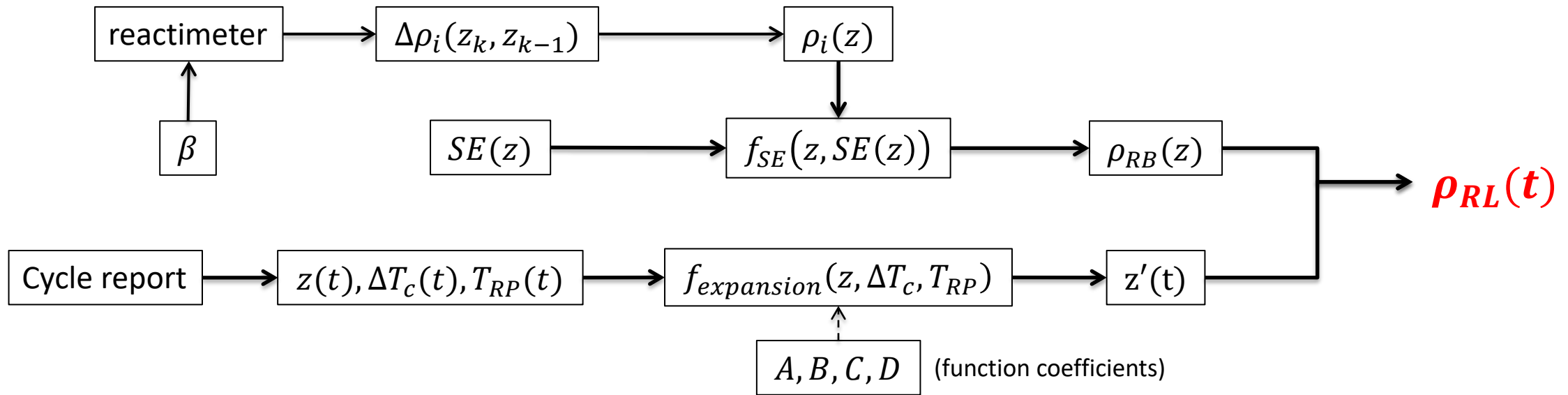


With all the  $\Delta\rho_i(z_k, z_{k-1})$  we can build  $\rho_i(z)$  for each control rod



# Experimental reactivity loss

## Global scheme of the reactivity loss curve construction

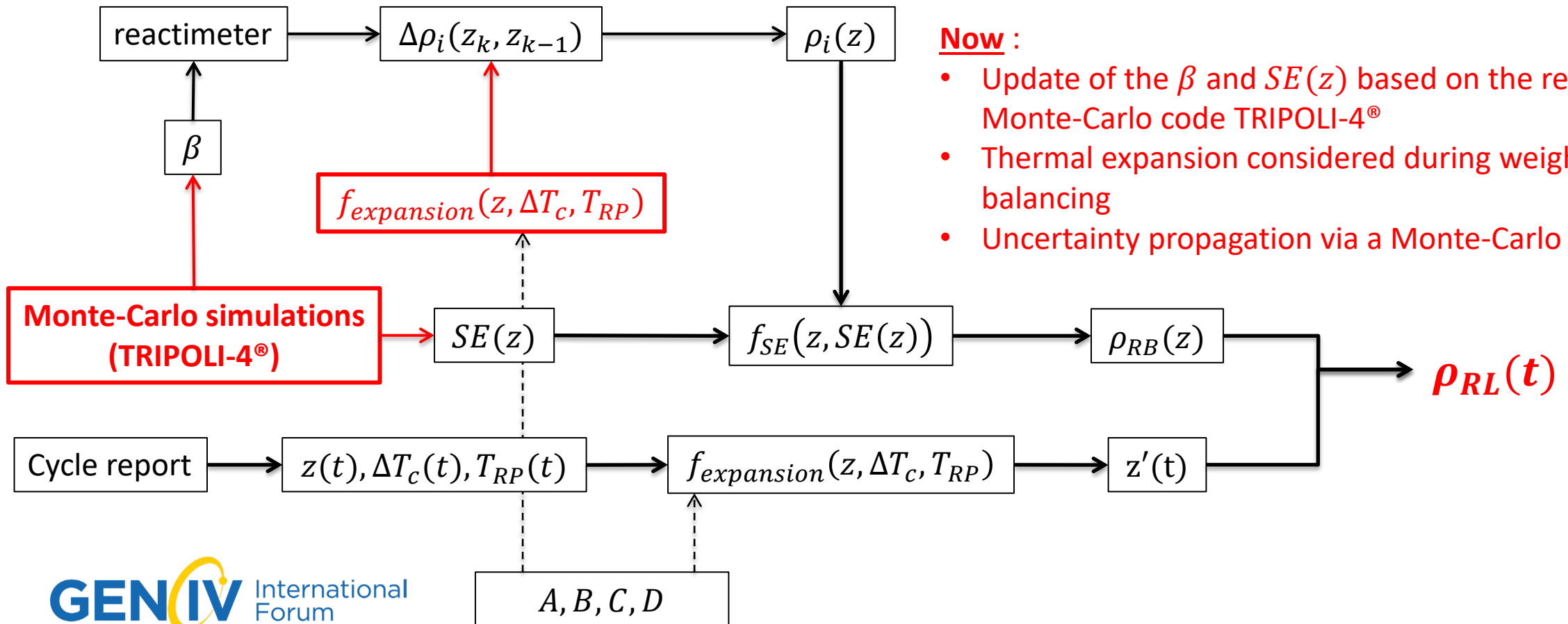


Before : Same  $\beta$  for every cycle |  $SE(z) = \text{cst}$  for every cycle | expansion not considered for weight balancing | **no uncertainty**

# Experimental reactivity loss

## Global scheme of the reactivity loss curve construction

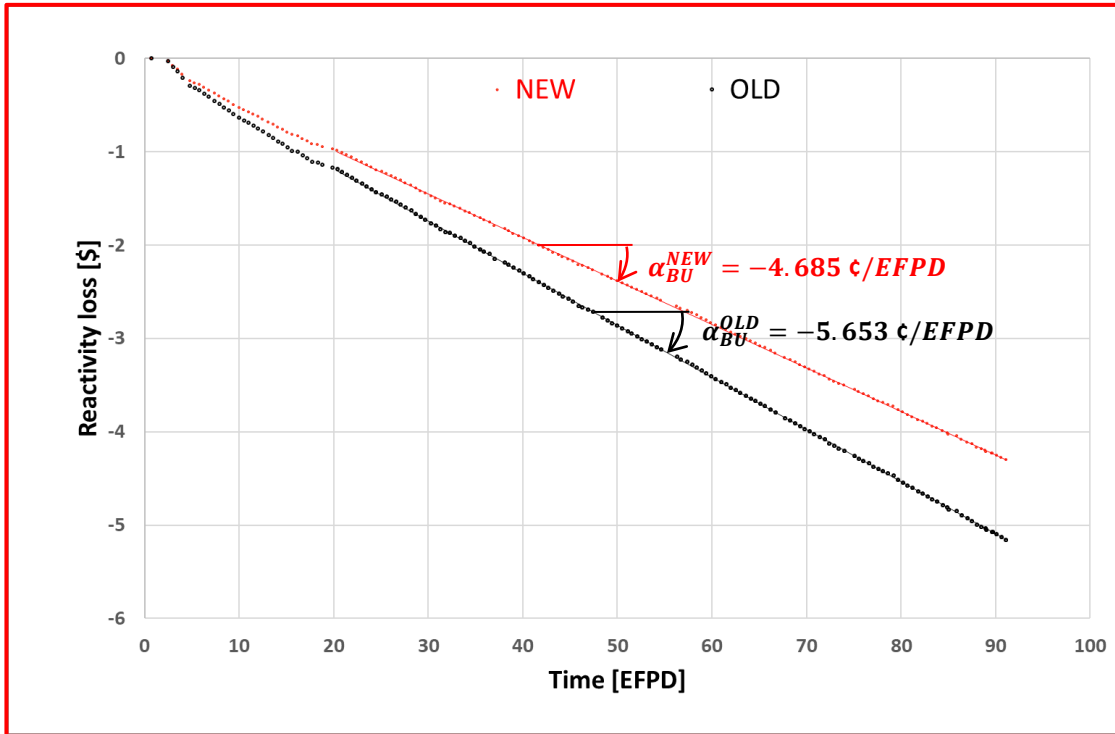
Before : Same  $\beta$  for every cycle |  $SE(z) = cst$  for every cycle | expansion not considered for weight balancing | **no uncertainty**



**Now :**

- Update of the  $\beta$  and  $SE(z)$  based on the reference Monte-Carlo code TRIPOLI-4®
- Thermal expansion considered during weight balancing
- Uncertainty propagation via a Monte-Carlo method

# Reactivity loss coefficient actualization



$$\alpha_{BU}^{OLD} = -5.653 \text{ ¢/EFPD}$$

$$\alpha_{BU}^{NEW_1} = -4.845 \text{ ¢/EFPD}$$

$$\alpha_{BU}^{NEW_2} = -4,578 \text{ ¢/EFPD}$$

$$\alpha_{BU}^{NEW} = -4.685 \text{ ¢/EFPD}$$

Updated Shadow-effect

Updated  $\beta$

Thermal expansion during weight balancing

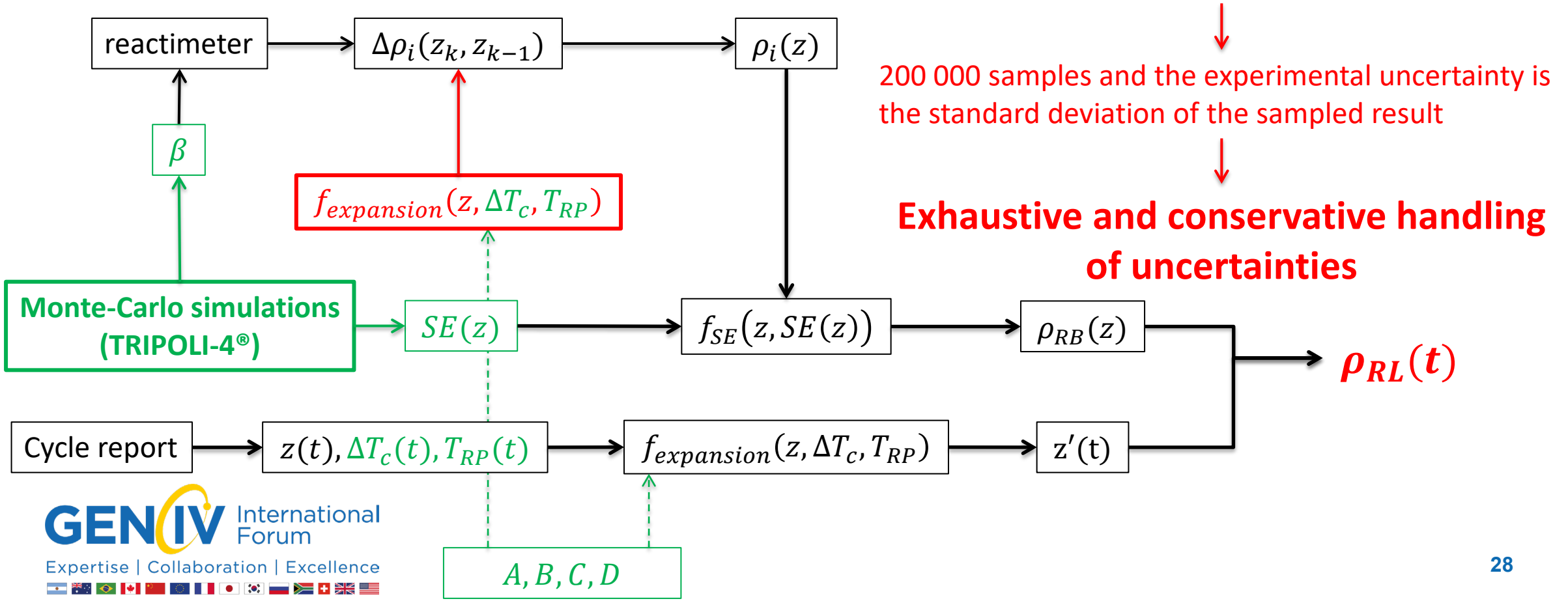
To be compared to

$$\alpha_{BU}^{DR-MP} = -4.650 \text{ ¢/EFPD}$$

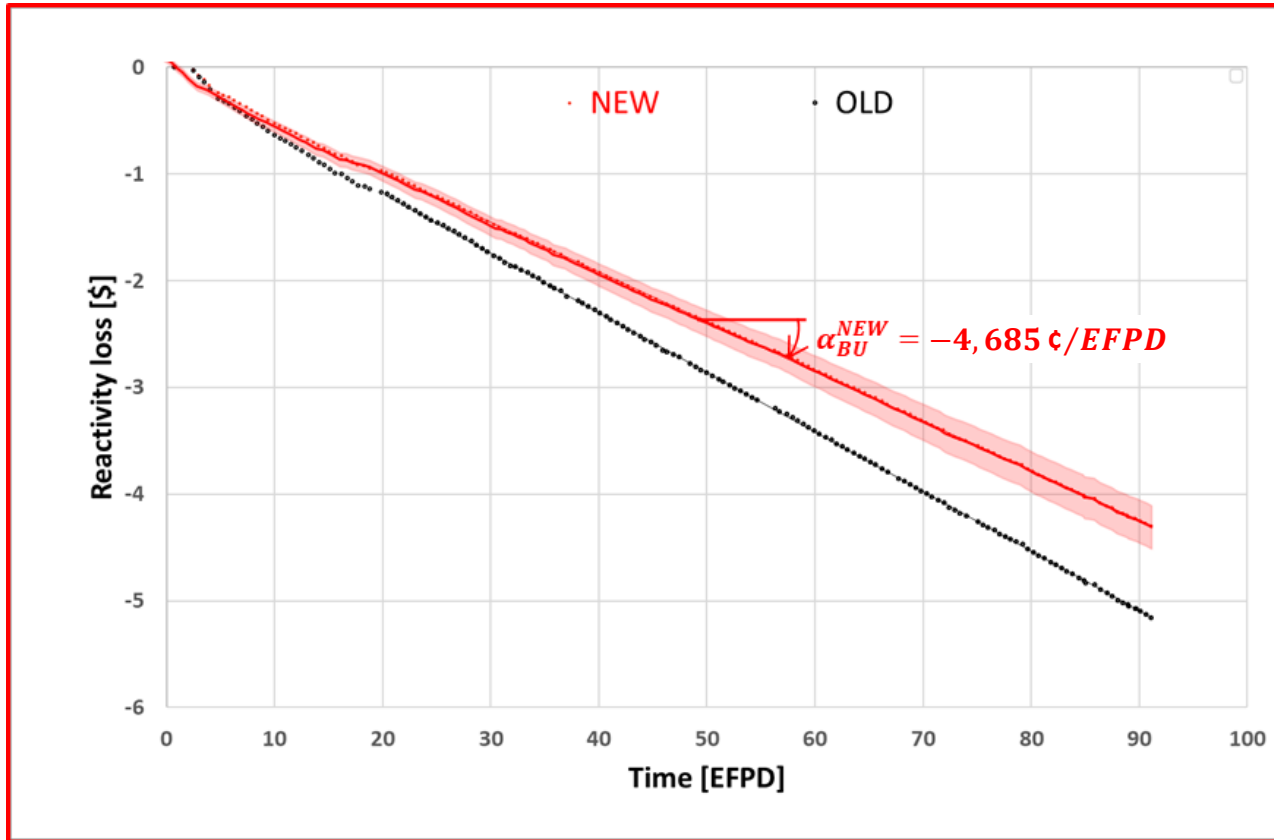
# Experimental reactivity loss

Uncertainty propagation via Monte-Carlo method = Sampling the input data with the related distribution

- For known uncertainties : correct distribution
- For unknown uncertainties : **conservative uniform distribution**



# Reactivity loss coefficient actualization



The most trustable value considering an exhaustive analysis

$$\alpha_{BU} = (-4.685 \pm 0.061) \text{ c/EFPD}$$

What about the power uncertainty ?

# Recap

Best-Estimate value:  $\alpha_{BU}^{DR-MP} = -4.650 \text{ ¢/EFPD}$

Bias decomposition:  $\Delta\alpha_{bias} \approx 0$  (to be investigated)

“Clean” Experimental value:  $\alpha_{BU}^{exp} = -4.685 \text{ ¢/EFPD}$

Conservative Experimental uncertainty:  $\Delta\alpha_{BU}^{exp} = 0.061 \text{ ¢/EFPD} \mid 1.3 \%$

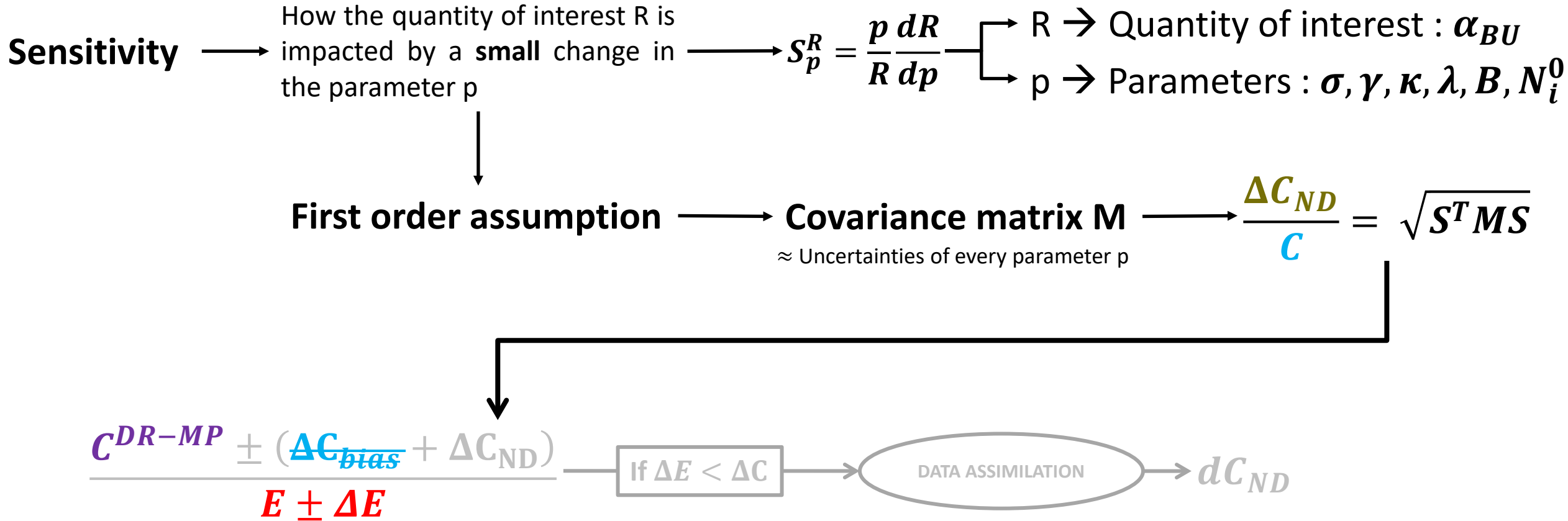
Nuclear data uncertainty:  $\Delta\alpha_{ND} = ?$



# 3 ■

## Reactivity loss nuclear data uncertainty propagation

# Reactivity loss sensitivity calculation





# How to compute the sensitivities

In neutronics it is possible to “easily” obtain the sensitivity to the  $k_{eff}$  of cross-section → **Perturbation Theory (PT)**

**Problems with local sensitivities computed with PT for depletion calculation?**

→ Only for direct term in the Boltzmann equation  
Not able to see all the indirect terms due to Bateman equation

For this kind of problems, specific formalism needs to be used → **Bateman/Boltzmann coupled sensitivities [Takeda, Williams in the 80’s]**

Compute by backtracking in time

$$S_p^R = \frac{1}{R} \left[ \underbrace{\left\langle p \frac{\partial R}{\partial p} \right\rangle}_{\text{Boltzmann (PT)}} + \underbrace{\int_{dt} \left\langle \mathcal{N}^* \left( \phi p \frac{\partial \mathcal{A}}{\partial p} \right) \mathcal{N} \right\rangle dt}_{\text{Bateman}} + \underbrace{P^* \left\langle p \frac{\partial P}{\partial p} \right\rangle}_{\text{Power}} + \underbrace{\left\langle \Gamma^* p \frac{\partial \mathcal{H}}{\partial p} \phi \right\rangle + \left\langle \Gamma p \frac{\partial \mathcal{H}^*}{\partial p} \phi^* \right\rangle}_{\text{Flux}} \right]$$

Implemented in **APOLLO-3®** and **first time** that this formalism is used on a **power reactor**

Finally, we don’t want exactly the sensitivity to the  $k_{eff}$  but to the reactivity loss between the BOC and the EOC

EGPT : Equivalent Generalized Perturbation Theory

$$S_{\Delta\rho_{A \rightarrow B}}^{EGPT} = \frac{k_A}{k_B - k_A} S_{k_B} - \frac{k_B}{k_B - k_A} S_{k_A}$$

# Uncertainty propagation

$$\frac{\Delta C_{DN}}{C} = \sqrt{{}^T S \cdot (M_{\sigma_{HN}} + M_{\sigma_{FP}} + M_{\gamma} + M_{\kappa} + M_{\lambda} + M_B) \cdot S}$$

$M_{\sigma_{HN}} + M_{\sigma_{FP}}$	→	COMAC V1 (experimental covariances)	$\sqrt{{}^T S M_{COMACV1} S} = 7.36 \%$
$M_{\gamma}$	→	<i>Variances / ad-hoc covariances*</i>	$\sqrt{{}^T S M_{\gamma} S} = 1.03 \%$
$M_{\lambda}$	→	Variances / no covariances	$\sqrt{{}^T S M_{\lambda} S} = 0 \%$
$M_B$	→	∅	≈ 0 %
$M_{\kappa}$	→	∅	≈ 0 %

**TOTAL Coupled sensitivities –  $\frac{\Delta C_{DN}}{C}$**                                       **7.43 %** (7 days of uncertainties for a 100 days cycle)

TOTAL Boltzmann alone –  $\frac{\Delta C_{DN}}{C}$     2.19 % (classical PT miss a large amount of information)

\*With the help of Luca Fiorito from SCK CEN

# Recap reactivity loss WVUQ

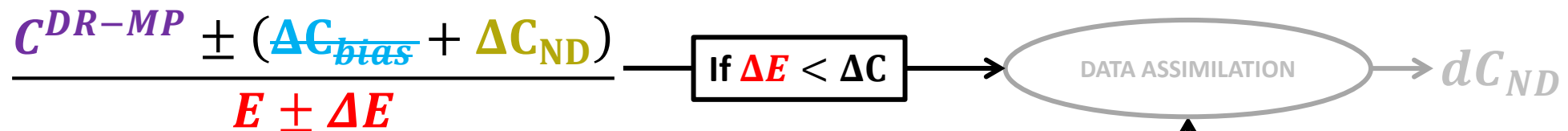
Best-Estimate value:  $\alpha_{BU}^{DR-MP} = -4.650 \text{ } \zeta/\text{EFPD}$

Bias decomposition:  $\Delta\alpha_{bias} \approx 0$  (to be investigated)

“Clean” Experimental value:  $\alpha_{BU}^{exp} = -4.685 \text{ } \zeta/\text{EFPD}$

Conservative Experimental uncertainty:  $\Delta\alpha_{BU}^{exp} = 0.061 \text{ } \zeta/\text{EFPD} \mid 1.3 \%$

Nuclear data uncertainty:  $\Delta\alpha_{ND} = 7.4 \%$



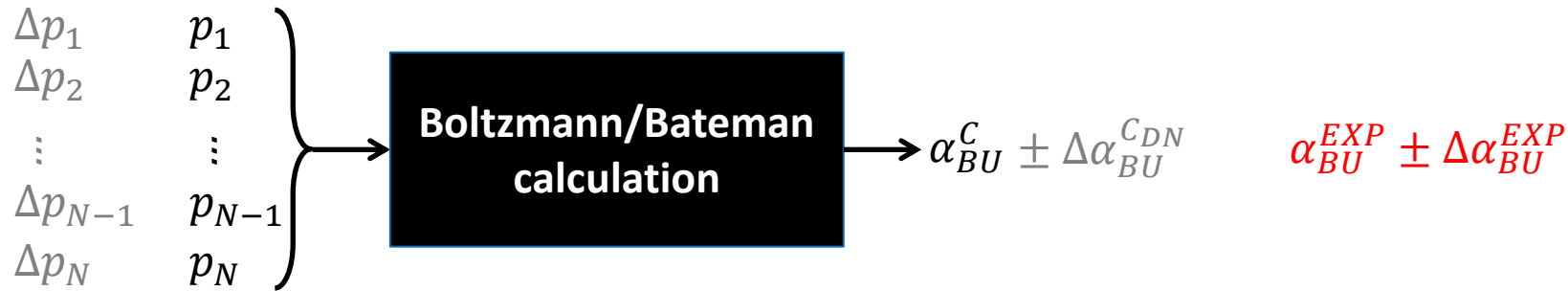
$$\frac{\Delta C_{ND} \text{ (Nuclear Data uncertainties)}}{\Delta C_{AP3} \text{ (epistemic uncertainties)}} \gg 1$$

# 4.

## Perspective on data assimilation using power reactor data

# Assimilation perspective

What is data assimilation ?  $\rightarrow$  Using the experimental value of an integral experiment to improve the knowledge of the input data = **Bayesian inference**



Assimilation process wants to find the set of  $p_i$  and  $\Delta p_i$  that allow to obtain :

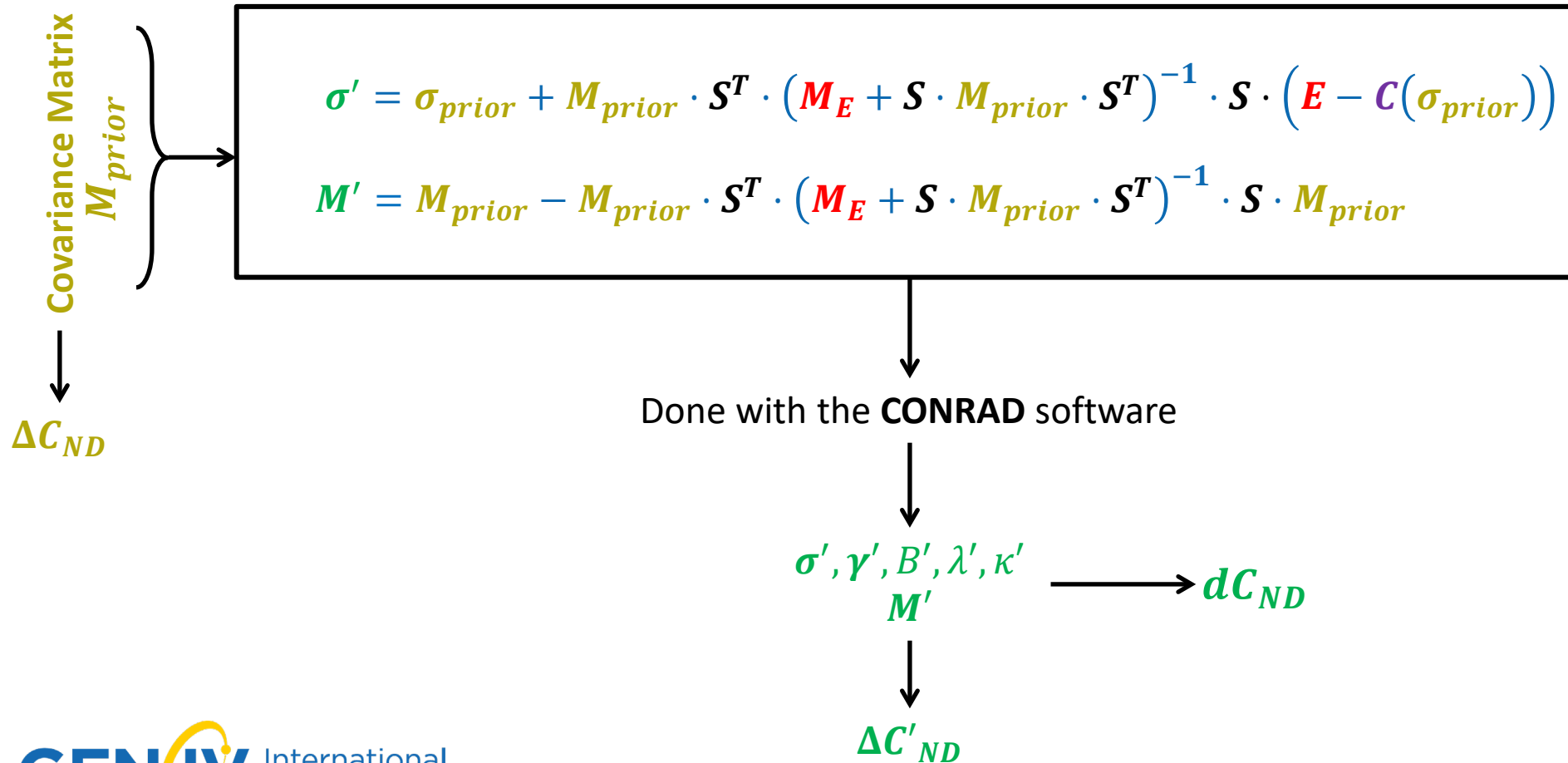
$\alpha_{BU}^C = \alpha_{BU}^{EXP}$  [correction of input data]  
 $\Delta \alpha_{BU}^{CDN} = \Delta \alpha_{BU}^{EXP}$  [uncertainty reduction of input data]

By respecting some physical and experimental constraints (covariance matrix) } **Minimization problem**

Problem : Optimization with brute force approach not reachable today (N > 10000)

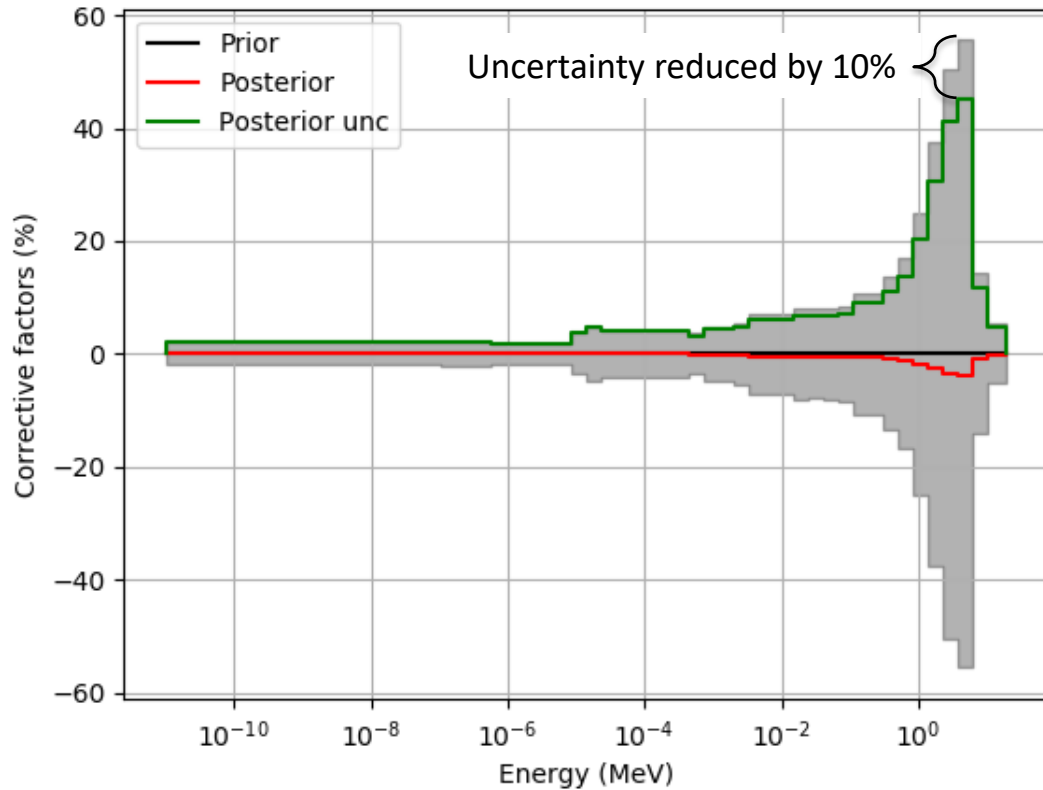
$\hookrightarrow$  But we can use **sensitivities**

# Assimilation perspective

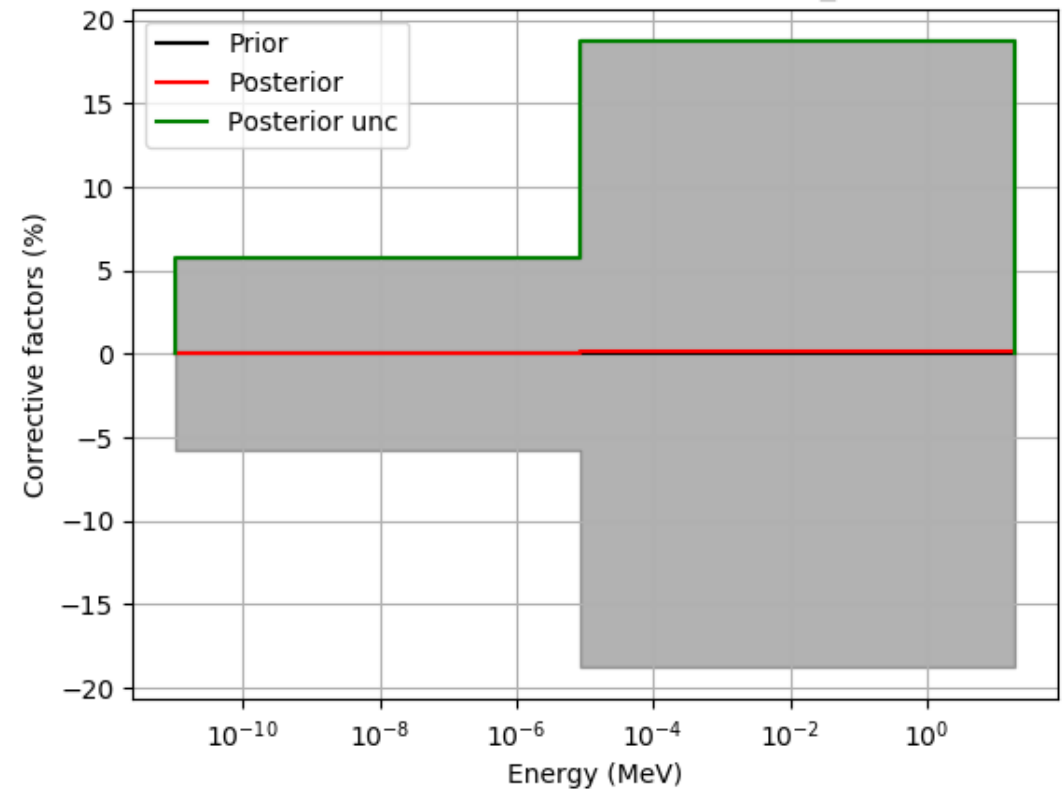


# Some results for data assimilation exercises

Data Assimilation of the  $^{240}\text{Pu}$  Capture



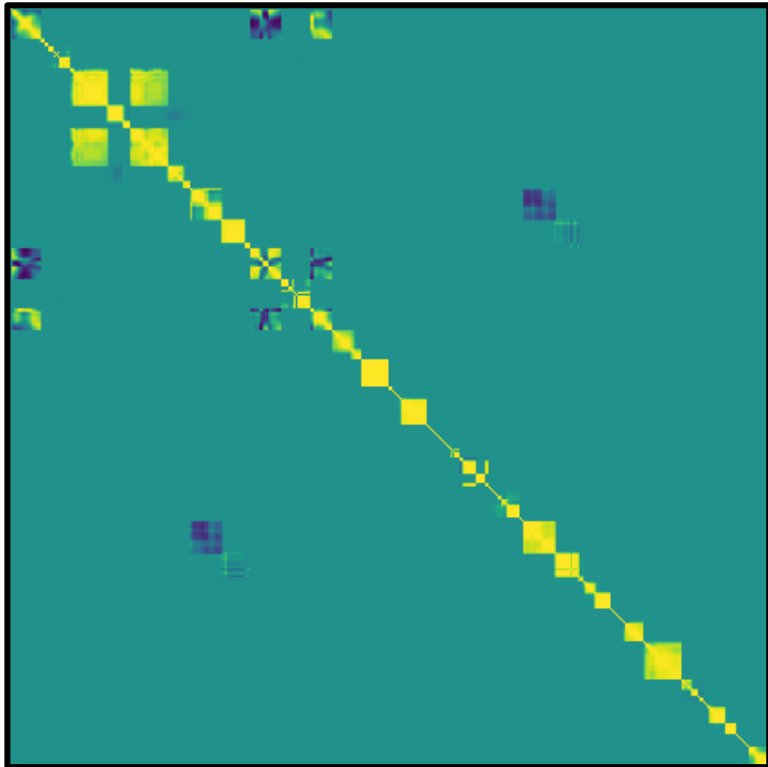
Data Assimilation of the  $^{239}\text{Pu} \rightarrow ^{107}\text{Pd}$  Fission Yield



$$\frac{C(\sigma_{prior})}{E} - 1 = -0.75\% \longrightarrow \frac{C(\sigma_{posterior})}{E} - 1 = -0.03\%$$

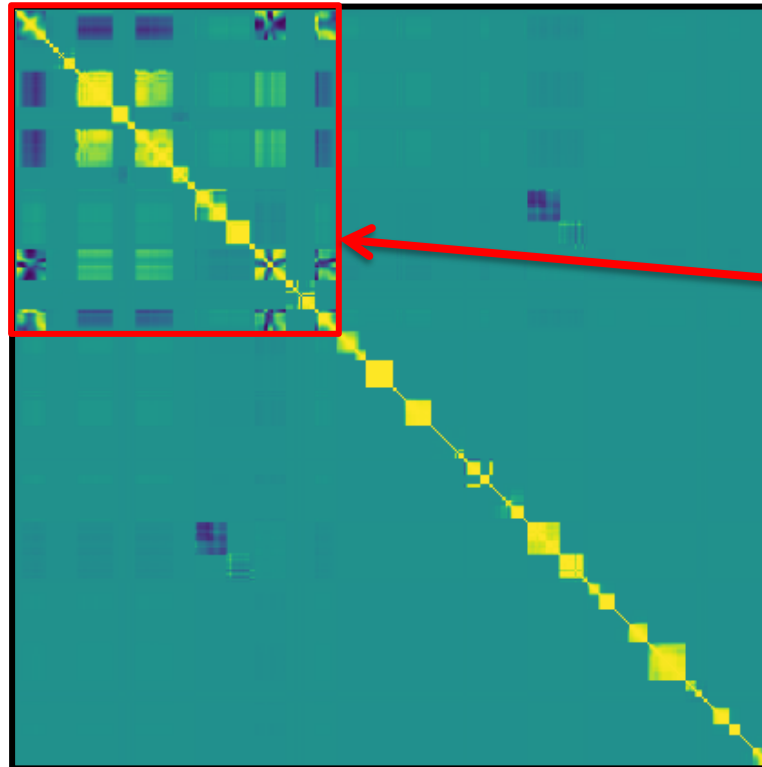
# Some results for data assimilation exercises

A priori correlation Matrix



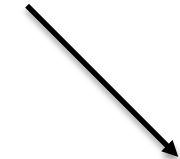
$$\Delta C_{ND} = 7.4\%$$

A posteriori correlation Matrix



$$\Delta C'_{ND} = 1.3\%$$

Largest contributor



Smallest contributor

Data assimilation mainly affects the six largest contributors

- $^{238}\text{U}$  Capture
- $^{240}\text{Pu}$  Fission
- $^{240}\text{Pu}$  Capture
- $^{239}\text{Pu}$  Capture
- $^{238}\text{U}$  Fission
- $^{238}\text{U}$  Inelastic

What is the physical value of those changes ?

How trustable is the initial correlation Matrix ?

How the initial correlation Matrix affect the result ?

...



# Conclusions/Perspectives

The development of future reactor has to rely on **validated** simulation tool with mastered and **quantified uncertainties**

New generation tools allow to extend the field of VVUQ to **power reactor** → it has been used for the **Phenix reactivity loss**

Starting from JEFF 3.1.1 with **7.4%** nuclear data uncertainties to **1.3%**

## Short term perspective

- Corrective factor
  - compare with trends from JEFF 4.
  - propagate to NDAST / ICSBEP / IRPhE to see the impact of such change
- Oriented further experiment towards some nuclear data
- Create adjusted cross-section on purpose (for a given reactor)

## Long term perspective

- Perform the same exercise with other power reactor (JOYO, VTR, EBR-II, ...)
- Uncertainty quantification + MP for core design purpose (lower the margins)

# Upcoming Webinars

Date	Title	Presenter
20 March 2024	Overview of Canadian R&D Capabilities to Support Advanced Reactors	Lori Walters, CNL, Canada
17 April 2024	Multiphysics Depletion & Chemical Analyses of Molten Salt Reactors	Samuel Walker, INL, USA
22 May 2024	Joint GIF/IAEA Webinar: Regulatory Activities in support of SMRs and Advanced Reactor Systems	<p>Panelists:</p> <ul style="list-style-type: none"> <li>• Ms. Paula Calle Vives, IAEA</li> <li>• Mr. Tarek Tabikh, CNSC</li> <li>• Dr. Greg Oberson, NRC</li> </ul> <p>Moderators:</p> <ul style="list-style-type: none"> <li>• Dr. Vladimir Kriventsev, IAEA</li> <li>• Dr. Patricia Paviet, PNNL</li> </ul>